Introduction

The STM32F373/378xx microcontrollers embed three Sigma-Delta Analog to Digital Converter (SDADC). This innovative ADC type offers specific properties to extend the application range.

The aim of this application note is to help understanding the SDADC principle, its properties and its features (explaining the functionalities), then compare SDADC with SAR type of ADC, and eventually help in choosing the correct ADC according to the addressed application.

The document includes:
- Overview of ADC types and their basic properties
- SDADC principle explained in a simple way
- SDADC advantages overview (from SDADC principle)
- Oversampling and Digital filter - explanation of this digital block and its implementation
- SDADC in STM32F373/378xx microcontrollers: summary of parameters
- How to read the ADC parameters: Guide to choose the correct ADC for each application.
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1 Introduction

ADC is the acronym for Analog to Digital Converter. It converts an analog voltage into digital code (Figure 1).

Figure 1. ADC function

1.1 ADC types

The main ADC function can be achieved using different techniques, each one with specific properties.

Most commonly ADC types (with their typical properties):

- Successive approximation ADCs (SAR ADC)
  - Middle / fast speed, middle resolution
- Flash ADC (Parallel ADC)
  - Fast speed, lower resolution
- Sigma-Delta ADC (SDADC)
  - Low / middle speed, high resolution, good linearity
- Integrated ADC (Dual slope ADC)
  - Low speed, middle resolution, good linearity
- Others …

ADC requirements:

They must be identified to use the correct ADC in each application:

- Resolution
  - Number of bits in the output
- Accuracy
  - Number of valid bits in the output
- Sampling rate
  - Sampling frequency of the input data signal
- Speed (output data rate)
  - Frequency at which the ADC digital output is updated
- Oversampling
  - Ratio between sampling rate and output data rate
- Errors
  - Static: Linearity (differential, integral, total), Offset, Gain, Quantization, Total error
  - Dynamic: THD, SNR, SINAD, ENOB (note: ENOB is a dynamic parameter)
2 SDADC overview

2.1 Basic principle

The SDADC basic principle can be divided into two parts:

- **Sigma-Delta modulation:**
  - Very fast sampling rate of analog signal but with only 1-bit resolution.
  - Result is a 1-bit data stream, where the long duration average value represents the analog input signal level (similar to PWM modulation). See *Figure 2*.

- **Digital filter:**
  - “Smart averaging” of the digital 1-bit data stream.
  - Result is higher resolution but lower data rate (oversampling + decimation).

*Figure 2. Sigma delta modulation (1-bit stream)*

*Figure 2* is an example of an analog input signal and its corresponding bit-stream on the Sigma-Delta modulator output.
2.2 Sigma-Delta modulator

A Sigma-Delta modulator is a circuit that generates a digital output with a 1-bit data stream from an analog input signal.

The output frequency isn’t constant (compared to PWM modulation), both frequency and duty cycle change.

**Figure 3. Sigma-Delta modulator diagram**

The principle of the first order Sigma-Delta modulator is shown in **Figure 3**. To better understand its operation, see **Figure 4** and **Figure 5**, that illustrate the voltage levels at different stages of the modulator.

**Figure 4** shows the Sigma-Delta modulator schematics.

The analog input signal [1] is added to the 1-bit DAC output (+V_ref or -V_ref voltage) fed back from the comparator and the result [2] goes to the integrator. The integrator output [3] is then compared with the zero level by the comparator. The comparator output [4] is latched periodically at the clock frequency by the D-latch to propagate the comparator result to the modulator output in quantized time steps (clock ticks). The D-latch output [5] is digital 1-bit output from the Sigma-Delta modulator. The output is fed back to the 1-bit D/A converter which has 2 analog output levels only (usually implemented as a switch between +V_ref and V_ref reference voltages). The data rate of the 1-bit output data stream is defined by the clock frequency.
Figure 4. Sigma-Delta modulator schematics

Figure 5. Sigma-Delta modulator timing diagram
2.3 Sigma-Delta principal advantages

2.3.1 Noise shaping

This section describes the difference between the spectrum of standard k-times oversampled SAR ADC (see Figure 6) and the spectrum of Sigma-Delta modulator (see Figure 7).

From Figure 6 it can be seen that the quantization noise is spread evenly over the whole Nyquist bandwidth (up to kF_s/2).

The digital filter removes noise above F_s/2. This noise suppression increases ADC resolution thanks to k-times oversampling.

**Figure 6. Oversampled SAR ADC spectrum**

![Figure 6](image)

*Figure 7 shows the Sigma-Delta modulator output spectrum (Spectrum of 1-bit data stream from modulator output from Figure 2). It can be seen that much of the noise is moved toward the high frequencies (thanks to the integrator used in the Sigma-Delta modulator).*

If an appropriate digital filter is used to filter 1-bit data stream then remaining noise is lower in comparison with SAR type ADC. The result is that oversampled Sigma-Delta modulation together with digital filtering can achieve better resolution than oversampled SAR ADC.

**Figure 7. Sigma-Delta modulator spectrum**

![Figure 7](image)
The noise spectrum shape comes directly from the Sigma-Delta modulation circuit. The 1-bit data stream result looks like PWM modulation and it has a variable frequency and duty cycle.

The Sigma-Delta modulator generates an output data stream with the highest possible frequency whereas PWM modulation has fixed frequency with variable duty cycle.

**Example 1**: 16-bit PWM

If the analog signal is at 50% of full scale then the 16-bit PWM modulation produces a signal with a 50% duty cycle at a fixed frequency: clock / 65536.

**Example 2**: Sigma-Delta modulator

If the analog signal is at 50% of full scale then the Sigma-Delta modulator in this case also produces a signal with 50% duty cycle but at the half clock frequency. As a consequence, the 1-bit data stream in the Sigma-Delta modulation has higher frequency content (especially if the analog signal is between 20%-80% of full scale, so that low duty cycle and therefore low frequency content is not generated). See Figure 8 and Figure 9. The advantage is easier design of the digital averaging filter to remove quantization noise.

**Figure 8. PWM modulation example**
2.3.2 Simpler anti-aliasing filter design

The sampling frequency ($F_s$) in the Sigma-Delta modulator is very high compared to the data bandwidth frequency ($F_{DATA}$) due to the oversampling technique: $F_s \gg F_{DATA}$.

The design of an anti-aliasing filter to reject high frequencies and meet the Nyquist criteria is therefore very simple and cheap.

*Figure 10* shows the cases of non-oversampled and oversampled ADC where the signal bandwidth is the same (same input signal) and the sampling frequency is $F_s$.

For non-oversampled ADC it is necessary to design a sharp filter roll-off to remove signals above frequency $F_s/2$. For the oversampled ADC (Sigma-Delta ADC) the design a simple lower order filter for $F_s/2$ image rejection is already sufficient.
Figure 10. anti-aliasing filter design

Nyquist rate sampling with $F_s > 2F_{\text{DATA}}$

Oversampling with $F_s >> 2F_{\text{DATA}}$

Anti-aliasing filter with sharp roll-off

Anti-aliasing filter with gradual roll-off

$F_s \sim 2F_{\text{DATA}}$

$F_s >> 2F_{\text{DATA}}$
3 Sigma-Delta ADC basic properties

3.1 Advantages

3.1.1 Excellent linearity

A Sigma-Delta modulator generates a stream with 1-bit output data width. This 1-bit data stream is converted into a multi-bit output using a linear filter - a mathematically exact linear operation.

The transfer characteristics between analog and digital values is therefore linear: each data word output is a multiple of this 1-bit weight, ensuring excellent linearity over the whole input range compared to other ADC types. Static linearity errors (differential and integral non-linearity) are therefore very low: DNL is ~0 (no missing codes), INL is lower than other ADC types.

An analog buffer can be used in front of Sigma-Delta modulator for high input impedance or to amplify the input analog signal. But this input buffer linearity influences the complete linearity of Sigma-Delta ADC.

Figure 11. Integral and differential linearities

The static parameter INL is linked to the dynamic THD parameter (total harmonic distortion). So THD is also very low for this ADC type. Remaining non-linearity is caused by non-ideal components used in the Sigma-Delta modulator (capacitors, comparator, resistors).

The low THD of the SDADC leads to its use for audio applications or any AC measurement applications sensitive to distortion.
3.1.2 Scalable final resolution

The SDADC final resolution depends only on the digital filter parameters (order, length, filter type). The filter averages the 1-bit input stream to a parallel output with lower data rate.

A longer averaging time results in a higher resolution (e.g. 24-bit ADC) - but the drawback of increased resolution is a lower output data rate and longer latency (time to first sample output).

Example: 24-bit output @ 1kHz output data rate, 16-bit output @ 50kHz output data rate.

For this reason SDADC converters are used for very precise lower frequency measurement or DC measurement applications - such resolution cannot be easily offered by other ADC types.

3.2 Disadvantages

3.2.1 Gain error

The output data word weight is a multiple of the 1-bit weight (see Section 3.1.1). This 1-bit weight depends on the Sigma-Delta modulator components (among them capacitors and resistors of the integrator), so the full scale weight is not related only to the reference voltage (as for example in a SAR type ADC).

Sigma-Delta modulator component parameters (R, C, ...) must be trimmed to produce full scale output data at full scale input analog signal ($V_{in} = V_{ref}$). This is a hard to achieve through RC trimming, as 1% error results in an overall gain error of some percent points. This error means that at full scale output, the input voltage is not exactly equal to the reference voltage (up to ~5% of difference).

This disadvantage can be corrected by software calibration of the gain of each device (gain error can vary from device to device due to modulator component tolerance). The output data word is recalculated according to the calibrated real gain.

3.2.2 Offset error

The output zero code of the SDADC doesn’t need to correspond to 0V at the input. The reason is due to the Sigma-Delta modulator components (integrator offset, comparator offset, 1-bit DAC symmetry).

The solution is again in the implementation of software (or hardware) calibration (adding a calibration offset constant to the output data result).

3.2.3 Lower data rate

For proper filtering of 1-bit samples to reach higher output resolution, the use of a digital filter with higher oversampling ratio and higher order is needed, this leads to lower output data rate (decimation). So a bargain must be struck between resolution and speed for a given application area. In general SDADCs are focused on lower data rate applications with higher resolution.
4 Digital filter - part of Sigma-Delta ADC

4.1 Function

The digital filter is part of the SDADC (see Figure 3). It performs filtering (averaging) of the 1-bit data stream generated from the Sigma-Delta modulator. The filter output is a data word with increased resolution (usually 12 - 24 bits) but reduced data rate (decimation).

4.2 Design

The filter design has a big impact on the SDADC characteristics and is a compromise between the required parameters and hardware implementation complexity (cost issue). The goal is to design the filter with minimum complexity while meeting the required SDADC parameters.

Note: The signal filtering is more complex than simply the averaging of the 1-bit data stream. Averaging is the simplest filtering implementation but in practice a more complex function is required (see Section 4.3).

4.2.1 Parameters

Filter type

Various filter types can be used, for cheap hardware implementation the Sinc filter (synchronous frequency response) has been developed. The Sinc filter is the most commonly used type in SDADC implementations. It is cheap because no multipliers are required, and filter coefficients are only integers.

Filter length

A longer filter (averaging of more samples) generates higher resolution but decreases output data rate (decimation).

Filter order

A higher order filter generates higher resolution (by adding more averaging loops) but increases filter initialization time (need to fill whole filter with samples to start to produce output data).

4.3 Digital filter - analysis

Parameters of the SDADC in the STM32F373/378xx (using fixed filter parameters):

- Sampling clock of Sigma-Delta modulator: $f_{in} = 6\ MHz$
- Final output data rate: $f_{out} = 50\ kHz$ (because of fixed decimation ratio = 120)
  \[ f_{out} = \frac{f_{in}}{120} \]
- Final resolution: 16 bits

When using simple averaging filter (first order Sinc filter) to reach a 16-bit resolution, 65536 bits have to be averaged using 1-bit data stream (see Figure 12). The output data rate will be $6\ MHz / 65536 = 91.6\ Hz$ only. To increase the data rate a more complex filter is required.
More complex filters (with higher order Sinc filter, where order ≥ 2) increase the final data rate with the same resolution. Higher order Sinc filters perform the moving average more times in chaining (averaging of averaged data from previous filter stage).

### Analysis of the higher order Sinc filter

The filtering now takes into account not only the number of ‘1s’ over a given duration (like simple averaging) but also their density in the data stream. This is thanks to the moving average implementation on each filter stage. Each filter stage is performing moving average over data from previous filter stage. At each cycle it performs the sum of the N values from previous stage outputs.

### Explanation of resolution increase with given number of samples in stream

- An N-bit long Sigma-Delta modulated bit stream is applied to the filter input.
- A small analog value is applied to the Sigma-Delta modulator input - to get a simple ‘1’ at the end of the data stream (at the N\(^{th}\) position - see top of Figure 13).
- When the analog value increases slightly, we get one ‘1’ in the middle of the data stream and one ‘1’ at the end of the data stream (see bottom of Figure 13).
- In the transition between these two analog values (see again Figure 13) is the ‘1’ bit moving from the N\(^{th}\) to the (N/2)\(^{th}\) position and then an additional ‘1’ appears at the end. (finally are there two bits in N-bit stream which represent higher analog value). Between those two states (on top and bottom of Figure 13) there are N/2 steps.
- So by recognizing position of this one ‘1’ (in which position it is on given N-bit stream) is obtained additional N/2 resolution between 2 consecutive original values. Between one bit per period and 2 bits per period (between values 1/65536 and 2/65536) there are N/2 additional recognized values.
- The complete resolution will be then: N * N/2 = N^2/2 (N is the length of the stream) because we added N/2 steps to original resolution (N). Stream length to achieve a 16-bit resolution will be: 65536 = N^2/2 → N = 362 bits.
Practical explanation of 3rd order filter with N=10 (moving averaging of each filter stage):

- A 3rd order filter with oversampling N=10 must be analyzed with 3 periods of input stream: 3xN = 30 samples (see Figure 14 and Figure 15).
- In input stream in each averaging period (N=10) there is only one '1' (see the "Input" curves). There are tested 2 input streams: one with higher pulse density (Figure 14) and another with slightly lower pulse density (Figure 15).
- First order filter is performing moving average (see the "1st order" curves) and final result is sampled each Nth cycle as 1st order filter result (at 10th, 20th, 30th cycle). It always produces '1' as the final result on both stream cases because of simple filter (only one '1' in each period).
- Second order filter is performing moving average on samples from first filter order (see the "2nd order /10" curves). Its final result is sampled each Nth cycle as 2nd order filter result (at 20th, 30th cycle). There is visible difference in final results between the two streams: due to higher density of '1's' (in higher density stream) it produces higher value than in lower density stream.
- Third order filter is performing moving average on samples from second filter order (see the "3rd order /100" curves). Its final result is sampled each Nth cycle as 3rd order filter result (at 30th cycle). There is visible difference in final result between higher density stream and lower density stream. Due to moving averaging the output is smoother and more precise.
Due to moving averaging in higher filter orders resolution can be increased with lower number of samples (N). The final resolution of filter with \( K \)th order is \( N^K \). But for higher order filter it is necessary to analyze stream with length \( K \times N \) to have final result because the given filter stage must be filled with valid samples from previous filter stage (see Figure 13). Therefore the effective resolution normalized to fixed sampling period is \( N^K / K \) (for one single conversion).

Higher order Sinc filters allow better operation over the data stream. They offer better resolution for a given stream duration or the same resolution for shorter stream duration. The drawback is more complex hardware design and longer initialization of the filter.

Figure 14. Example of 3rd filter order outputs with Input higher

![Graph showing higher density of input pulses for higher orders of the filter.](image)

Figure 15. Example of 3rd filter order outputs with Input lower

![Graph showing lower density of input pulses for higher orders of the filter.](image)

Note: Data streams containing 10% to 90% of '1s' should be input to the digital filter – to have enough '1s' or '0s' to ensure proper filtering (so usually nominal input range is 10-90% of max. input range: all '0s' or all '1s'). N-bit stream containing more '1s' and '0s' has higher
frequency content spectrum and is more suitable for low pass filtering (see Figure 7, frequencies are filtered out).

Note: When starting filter operation fresh data should be input to the full filter to start generating valid output from a valid input data ("filter order" x "filter length" bits). The first sample is therefore delayed. Then in continuous operation mode is output data rate faster (each "filter length" bits) because filter is already filled with immediate valid previous data.

4.4 Digital filter – HW design basics

The following section describes in a simple manner the hardware design of a higher order Sinc filter. The explanation is divided into several steps to better understand the final implementation schematic.

4.4.1 Basic averaging

The main function is to average FOSR (filter oversampling ratio) 1-bit samples from input 1-bit data stream. This averaging needs to be performed at each sampling clock cycle. It can be described by the equation:

\[ y(n) = x(n) + x(n-1) + x(n-2) + ... + x(n-(\text{FOSR} - 1)) \]

Where:
- \( x(n) \) is the input of \( n^{\text{th}} \) sample;
- \( y(n) \) is the output of \( n^{\text{th}} \) sample;

Drawback of this hardware implementation is that there is required (see Figure 16):
- \((\text{FOSR} - 1)\) adders
- \((\text{FOSR}-1)\) flip-flops

\[ y(n) = x(n) + x(n-1) + ... + x(n-(\text{FOSR} - 1)) \]

\[ x(n) \]
\[ x(n-1) \]
\[ x(n-2) \]
\[ x(n-(\text{FOSR} - 1)) \]

\[ y(n) \]

Figure 16. Schematic of implementation - 1

4.4.2 Simplification of schematic

In the original schematic a lot of previous samples need to be stored in flip-flops. This can be simplified by using the previous result \( y(n-1) \).
The output $y(n)$ at sample instant $n$ is given by:

$$y(n) = x(n) + x(n-1) + x(n-2) + \ldots + x(n - (\text{FOSR} - 1))$$

So if the previous output at sample instant $n-1$ is given by:

$$y(n-1) = x(n-1) + x(n-2) + \ldots + x(n - (\text{FOSR} - 1)) + x(n - \text{FOSR})$$

Then original equation can be simplified to:

$$y(n) = x(n) + y(n-1) - x(n - \text{FOSR})$$

or

$$y(n) = x(n) - x(n - \text{FOSR}) + y(n-1)$$

The simplified schematic (Figure 17) is then described by equation:

$$y(n) = p(n) + y(n-1) \quad \text{where:} \quad p(n) = x(n) - x(n - \text{FOSR})$$

**Figure 17. Schematic of implementation - 2**

![Schematic of implementation - 2](https://via.placeholder.com/150)

**Improvement and drawback (Figure 17):**
- with only 2 adders
- but still needed (FOSR+N) flip-flops

### 4.4.3 Z-domain analysis

The first order Sinc filter difference equation is:

$$y(n) = x(n) - x(n - \text{FOSR}) + y(n-1)$$

To convert this into a different equation in discrete time domain, we can use the following correspondences:

- $X(z)$... in the Z-domain corresponds to $x(n)$ in the discrete time domain, where $n$ is an integer number of sample clock periods $\tau = 1/Fs$
- $z^{-N}X(z)$... corresponds to $x(n-N)$ - which is $x(n)$ delayed by $N$ sample periods.

Transfer function $H(z)$ for a 1-st order Sinc filter in Z-domain:
From Figure 17, we can see that the left-hand "comb" stage is cascaded with right-hand "integrator" stage (therefore the name of this filter type is CIC filter: Cascaded integrator-comb filter).

The comb transfer function in Z-domain is:

$$H_C(z) = \frac{P(z)}{X(z)} = 1 - z^{-FOSR}$$

The integrator transfer function is:

$$H_I(z) = \frac{Y(z)}{P(z)} = \frac{1}{1 - z^{-1}}$$

The overall transfer function is equivalent to the Sinc filter transfer function:

$$H(z) = H_C(z) \cdot H_I(z) = \frac{Y(z)}{X(z)} = \frac{(1 - z^{-FOSR}) \cdot \left(\frac{1}{1 - z^{-1}}\right)}{1 - z^{-FOSR}} = H(z)$$

In the next one will be explained how the design can be simplified. Firstly it is possible to reverse the order of the comb and integrator operation (integrator first):

$$H(z) = H_I(z) \cdot H_C(z) = \frac{1}{1 - z^{-1}} \cdot (1 - z^{-FOSR})$$

The reordered schematic is shown in Figure 18.

Figure 18. Reordered schematic (integrator stage as first)

The next step of simplification is to down-sample the output $y(n)$ by FOSR factor because the filtering limits the output signal bandwidth and so the output sampling rate can be reduced. This down-sampling is achieved by taking one sample of $y(n)$ every FOSR clock cycles (see Figure 19.).
The down-sampled clock period is defined as:

$$T = \frac{\text{FOSR}}{F_s} = \text{FOSR} \cdot \tau$$

where: $$\tau = \frac{T}{\text{FOSR}}$$

The difference equation for the down-sampled comb section can be rewritten:

$$y(n \cdot \tau) = p(n \cdot \tau) - p(n \cdot \tau - \text{FOSR} \cdot \tau)$$

$$y(n \cdot \frac{T}{\text{FOSR}}) = p(n \cdot \frac{T}{\text{FOSR}}) - p(n \cdot \frac{T}{\text{FOSR}} - \frac{\text{FOSR} \cdot T}{\text{FOSR}})$$

$$y(m) = p(m) - p(m - 1)$$

where: $$m = \frac{n}{\text{FOSR}}$$

This operation corresponds to a down-sampling of $p(n)$ by FOSR, followed by a first order differentiator (comb part simplification). So the final schematic for N-bit output data width (see Figure 20.) is reduced to:

- $2 \cdot N$ flip-flops (N ... output data bit-width)
- 2 adders (each with N-bit width)

Figure 20. Final schematic of first order CIC filter

### 4.4.4 Higher order CIC filters

In the previous section has been analyzed a first order CIC (Sinc) filter. To improve the resolution the filters can be cascaded.
For a $K$th order Sinc filter the transfer function is:

$$H(z) = \frac{Y(z)}{X(z)} = \left(\frac{1-z^{-\text{FOSR}}}{1-z^{-1}}\right)^K = \left(\frac{1-z^{-\text{FOSR}}}{1-z^{-1}}\right) \cdot \left(\frac{1-z^{-\text{FOSR}}}{1-z^{-1}}\right) \cdots$$

This can be viewed as a cascade of first order filters, each one being a cascade of an integrator part with a comb part:

$$H(z) = \left[\left(\frac{1}{1-z^{-1}}\right) \cdot \left(1-z^{-\text{FOSR}}\right)\right] \cdot \left[\left(\frac{1}{1-z^{-1}}\right) \cdot \left(1-z^{-\text{FOSR}}\right)\right] \cdots$$

By reordering into a group of integrators and a group of comb parts:

$$H(z) = \left[\left(\frac{1}{1-z^{-1}}\right) \cdot \left(\frac{1}{1-z^{-1}}\right) \cdots\right] \cdot \left[(1-z^{-\text{FOSR}}) \cdot (1-z^{-\text{FOSR}}) \cdots\right]$$

For decimation, the down-sampling is performed at the output of the final integrator stage, allowing to replace each comb stage with a unity delay differentiator at the down-sampled rate (see Figure 21.).

**Figure 21. Higher order CIC filter implementation**
5 SDADC in STM32F373/378xx

5.1 SDADC peripheral description

5.1.1 SDADC from HW design

In the STM32F373/378xx device there are three ADCs based on the Sigma-Delta principle (SDADC1, SDADC2, SDADC3). From a hardware point of view these SDADCs have the following designed parameters:

- Resolution: 16 bits
  - output data bit width
- ENOB = ~12.3 bits (gain=1), ~13.8 bits (gain=8)
  - dynamic parameter representing AC performance of SDADC
- Input sampling rate (sigma delta modulator clock, SDADC clock):
  - max. 6 MHz
  - min. 0.5 MHz
- Speed (output data rate):
  - max. 50 kHz
- Sinc filter:
  - Oversampling ratio: FOSR = 120 (fixed)
  - Order: K = 3 (fixed)
- Gains:
  - Analog gains: 0.5, 1, 2, 4, 8
  - Digital gains: 16, 32
- Offset calibration:
  - Internal offset measurement when inputs are shorted
  - Offset stored in register and used as correction
- Power supply:
  - Independent analog supply pins (2 independent supplies for three SDADCs)
  - \( V_{DDSDx} = 2.4 \, \text{V} - 3.6 \, \text{V} \) (or 2.2 V for clock <1.5MHz)
  - Consumption: 1200 / 600 / 200 / 2.5 / 1 \, \mu\text{A} (fast / slow / standby / power down / SDADC off)
- Reference voltage:
  - External source: on VREFSD+ pin (VREFSD = 1.1 V - VDDSDx)
  - Internal sources:
    - Embedded internal reference: \( V_{REFINT} = 1.2 \, \text{V} \) (or 1.5x amplified: 1.8 V)
    - SDADC power supply as reference: VDDSDx
- Input impedance:
  - Switched capacitor character (depends from selected SDADC clock and analog gain):
    - \( 47k\Omega \) ... @6MHz, gain=8
    - \( 68k\Omega \) ... @6MHz, gain=1
    - \( 540k\Omega \) ... @1.5MHz, gain=0.5
5.1.2 **SDADC precision characteristics overview**

SDADCs in STM32F373/378xx reached following precision performance:

- **Static parameters:**
  - Offset: ~100 µV
  - Gain error: ~3%
  - Differential non linearity (DNL): ~2.5 LSB
  - Integral non linearity (INL): ~15 LSB

- **Dynamic parameters:**
  - Total harmonic distortion (THD): ~ -77dB (gain = 1)
  - Signal to noise ratio (SNR): 88dB (gain = 1)
  - Signal to noise and distortion ratio (SINAD): 77dB (gain = 1), 85dB (gain=8)
  - Effective number of bits (ENOB): ~12.5 bits (gain=1), ~13.8 (gain=8)

5.2 **SDADC applications with STM32F373/378xx**

Integrated SDADC converters in STM32F373/378xx device are suitable for applications with some of following needs:

- **higher analog precision:**
  - (more than the internal 12-bit SAR ADC)

- **lower frequency signals (audio range, DC measurement):**
  - DC measurements
  - audio frequency range signals

- **small signal levels measurement:**
  - integrated analog gains up to 8x

- **differential measurements:**
  - differential inputs into ADC (“plus” and “minus” input pins)

- **linear**
  - audio applications for lower distortion

Examples of applications are:

- DC sensors measurement (thermometers, pressure sensors, ...)
- audio recording (with ensuing Cortex®-M4 core computation power postprocessing)
- electricity meters (electric current measurement in a wide range)
- medical applications (ECG sensors, ...)
- industrial applications (motor controls, sensors, ...)
- All applications which require higher ADC precision, not so fast, lower signal measurement together with fast digital data post-processing featured by STM32F373/378xx (Cortex®-M4 core with DSP instructions and FPU)
6 ADC parameters and their importance in different applications

Each ADC is characterized by several parameters which describe its electrical characteristics and accuracy. The suitability of a given ADC for a specific application should be determined according to these parameters. Therefore there is the need to know how to read each ADC parameter with respect to the given application needs, and, vice versa, for a given application there is need to focus on important ADC parameters only.

The following section describes how to perform correct ADC parameters selection for several practical applications.

The first step of ADC selection is the analysis of the electrical characteristics. According to the application needs, the correct ADC can be chosen which fulfills those requirements or which can be adapted to those requirements (usually by adding external components).

6.1 Basic ADC electrical characteristics

The basic parameters are:
- supply voltage range
- input analog voltage range
- input impedance (and its dependency on voltage/clock/...)
- conversion speed
- reference voltage parameters (external/built in, range, ...)
- consumption
- startup time

6.2 Static ADC parameters

These parameters are important for DC measurements:
- linearity (INL, DNL)
- offset
- gain error
- resolution
- stability (temperature, time)
6.3 Dynamic ADC parameters

These parameters are important for AC measurements:
- ENOB (effective number of bits in AC signal reconstruction)
- distortion of signal (THD), intermodulation distortion (IMD)
- noise (SNR, SINAD, NPR)
- frequency bandwidth (ADC speed)
- channel crosstalk
- spurious free dynamic range (SFDR)
- differential gain error (DG), differential phase error (DP)

6.4 Typical ADC application guide

*Table 1* contains a list of often used ADC applications areas and corresponding important parameters to check, as well as their impact on the application

<table>
<thead>
<tr>
<th>Typical applications</th>
<th>Critical ADC parameters</th>
<th>Performance issues</th>
</tr>
</thead>
<tbody>
<tr>
<td>Audio</td>
<td>SINAD, THD, noise.</td>
<td>- Power consumption.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>- Crosstalk and gain matching.</td>
</tr>
<tr>
<td>Automatic control</td>
<td>Monotonicity.</td>
<td>- Transfer function.</td>
</tr>
<tr>
<td></td>
<td>Short-term settling, long-term stability, noise.</td>
<td>- Crosstalk and gain matching.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>- Temperature stability.</td>
</tr>
<tr>
<td>Data acquisition</td>
<td>DNL, INL, gain, offset, noise, out-of-range recovery, settling time, full-scale step response, channel-to-channel crosstalk.</td>
<td>- Channel-to-channel interaction.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>- Accuracy, traceability (Sol Max).</td>
</tr>
<tr>
<td>Digital oscilloscope/waveform recorder</td>
<td>SINAD, ENOB, noise.</td>
<td>- SINAD for wide bandwidth amplitude resolution.</td>
</tr>
<tr>
<td></td>
<td>Bandwidth.</td>
<td>- Low thermal noise for repeatability.</td>
</tr>
<tr>
<td></td>
<td>Out-of-range recovery.</td>
<td>- Bit error rate.</td>
</tr>
<tr>
<td>Geophysical</td>
<td>THD, SINAD, long-term stability, noise.</td>
<td>- Millihertz response.</td>
</tr>
<tr>
<td>Imaging</td>
<td>DNL, INL, SINAD, ENOB, noise.</td>
<td>- DNL for sharp-edge detection.</td>
</tr>
<tr>
<td></td>
<td>Out-of-range recovery.</td>
<td>- High-resolution at switching rate.</td>
</tr>
<tr>
<td></td>
<td>Full-scale step response.</td>
<td>- Recovery from blooming.</td>
</tr>
<tr>
<td>Radar and sonar</td>
<td>SINAD, IMD, ENOB.</td>
<td>- SINAD and IMD for clutter</td>
</tr>
<tr>
<td></td>
<td>SFRD.</td>
<td>- cancellation and Doppler processing.</td>
</tr>
<tr>
<td>Spectrum analysis</td>
<td>SINAD, ENOB.</td>
<td>- SINAD and SFDR for high linear dynamic range measurements.</td>
</tr>
</tbody>
</table>
### Table 1. Critical ADC parameters\(^{(1)}\) (continued)

<table>
<thead>
<tr>
<th>Typical applications</th>
<th>Critical ADC parameters</th>
<th>Performance issues</th>
</tr>
</thead>
<tbody>
<tr>
<td>Spread spectrum communication</td>
<td>SINAD, IMD, ENOB, SFDR, NPR. Noise-to-distortion ratio, noise.</td>
<td>– IMD for quantization of small signals in a strong interference environment. – SFDR for spatial filtering. – NPR for interchannel crosstalk.</td>
</tr>
<tr>
<td>Telecommunication personal communications</td>
<td>SINAD, NPR, SFDR, IMD. Bit error rate. Word error rate, noise.</td>
<td>– Wide input bandwidth. – Interchannel crosstalk. – Compression. – Power consumption.</td>
</tr>
<tr>
<td>Video</td>
<td>DNL, SINAD, SFDR, DG, DP, noise.</td>
<td>– Differential gain and phase errors. – Frequency response.</td>
</tr>
<tr>
<td>Wideband digital receivers</td>
<td>SFDR, IMD. SINAD, noise.</td>
<td>– Linear dynamic range for detection of low-level signals in a strong interference environment. – Sampling frequency.</td>
</tr>
</tbody>
</table>

COMINT = communications intelligence  
DG = differential gain error  
DNL = differential nonlinearity  
DP = differential phase error  
ELINT = electronic intelligence  
ENOB = effective number of bits  
IMD = intermodulation distortion  
INL = integral nonlinearity  
NPR = noise power ratio  
SFDR = spurious free dynamic range  
SIGINT = signal intelligence  
SINAD = signal-to-noise-and-distortion ratio  
THD = total harmonic distortion

\(^{(1)}\) Table taken from: IEEE Std 1241-2010, IEEE Standard for Terminology and Test Methods for Analog-to-Digital Converters
7 Revision history

Table 2. Document revision history

<table>
<thead>
<tr>
<th>Date</th>
<th>Revision</th>
<th>Changes</th>
</tr>
</thead>
<tbody>
<tr>
<td>30-Jul-2015</td>
<td>1</td>
<td>Initial release.</td>
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</table>